## Momentum & Center of Mass

If all three collisions in the figure shown here are totally inelastic, which bring(s) the car on the left to a halt?



Think fast! You've just driven around a curve in a narrow, one-way street at 25 mph when you notice a car identical to yours coming straight toward you at 25 mph.You have only two options: hitting the other car head on or swerving into a massive concrete wall, also head on. In the split second before the impact, you decide to

- (1) hit the other car.
- (2) hit the wall.
- (3) hit either one—it makes no difference.
- (4) consult your lecture notes.

Suppose you are on a cart, initially at rest on a track with very little friction. You throw balls at a partition that is rigidly mounted on the cart. If the balls bounce straight back as shown in the figure, is the cart put in motion?



- 1. Yes, it moves to the right.
- 2. Yes, it moves to the left.
- 3. No, it remains in place.

Suppose the entire population of the world gathers in one spot and, at the sounding of a prearranged signal, everyone jumps up. While all the people are in the air, does Earth gain momentum in the opposite direction?

(1) No; the inertial mass of Earth is so large that the planet's change in motion is imperceptible.

(2) Yes; because of its much larger inertial mass, however, the change in momentum of Earth is much less than that of all the jumping people.

(3) Yes; Earth recoils, like a rifle firing a bullet, with a change in momentum equal to and opposite that of the people.

(4) It depends.

Suppose rain falls vertically into an open cart rolling along a straight horizontal track with negligible friction. As a result of the accumulating water, the kinetic energy of the cart:

(1) increases.

(2) does not change.

(3) decreases.

Consider two carts, of masses m and 2m, at rest on an air track. If you push first one cart for 3 s and then the other for the same length of time, exerting equal force on each, the momentum of the light cart is

- (1) four times
- (2) twice
- (3) equal to
- (4) one-half
- (5) one-quarter

the momentum of the heavy cart.



Consider a letter "C" that is obtained by cutting a large square plate  $2a \times 2a$  and removing a square  $a \times a$  from the side, as shown in the sketch. Determine the x coordinate of the center of mass,  $x_{CM}$ :

(1) (2) (3)  
$$x_{CM} < a \quad x_{CM} = a \quad x_{CM} > a$$